## Quiz 1 (Open Book/Notes)

## Solution

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## Honor Code Pledge

The information provided in this exam is my own work. I have not received information from another person while doing this exam.
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## Problem \#1 (50 points)

The Los Angeles Airport Authority would like to request your services to study runway length improvements to runway 24R on the North side of the airport. Review Airnav and the satellite images at Google Earth to answer the following questions. The airport authority is to improve runway 24R allowing airlines to support international services and also to serve and some long-distance domestic destinations. Estimate the runway extension needed for runway $06 \mathrm{~L} / 24 \mathrm{R}$ if the critical stage length services have been identified at this airport for various airlines (see Table 1).

More detailed information about the airport can be found at the AIRNAV database available on the web at: http://www.airnav.com/ airports/. In your analysis use the latest version of the Boeing and Airbus documents for airport design (http://128.173.204.63/ courses/cee5614/sites_ce_5614.htm|\#Aircraft_Data).

Table 1. Typical Services from LAX to Other Airports Needed to Support Runway 24R Operations.

| Origin-Destination Airport Pair | Aircraft Flying the Route |
| :--- | :--- |
| KLAX - LIM <br> Los Angeles - Lima (Peru) | Boeing 767-400ER with CF6-80C2B8 engines. Aircraft maximum <br> design takeoff weight is 450,000 lb. Aircraft has a typical three- <br> class configuration. |
| KLAX - HKG <br> Los Angeles - Hong Kong | Boeing 777-300ER powered by two GE90/115BL engines rated at <br> $115,000 \mathrm{lb}$ of thrust. Aircraft maximum takeoff weight is 766,000 <br> lb. Three-class layout. |

a) Find the average stage length to be flown between each one of the critical OD airport pairs. In your analysis use the Great Circle Flight Path mapper link provided in our interesting web sites (see below). Add $5 \%$ to the distances calculated to account for real Air Traffic route conditions and to account for possible weather deviations from the optimal flight path.

## Table 1a. Stage Length for Flights.

| OD Pair | GCD Route (nm) | Planned Route (nm) |
| :--- | :--- | :--- |
| LAX-LIM | 3,621 | 3,802 |
| LAX-HKG | 6,309 | 6,624 |

b) Find the runway length needed for each one of the three routes. Determine which one of the three trips constitutes the critical stage length and design the new runway length extension needed. Comment on your solution.

Table 1b. LAX-LIM Flight. Boeing 767-400ER with General Electric CF6-80C2B8 Engines. 3,802 nm Planned Route Distance.

| Parameter | Value (kg) | Remarks |
| :---: | :---: | :---: |
| MTOW | 204,116 | Table 2.1.6 per Boeing Specification |
| MALW | 158,757 | Table 2.1.6 |
| OEW | 103,147 | Table 2.1.6 |
| Max. Payload | 46,538 | Table 2.1.6 |
| Usable Fuel | 73,363 | Table 2.1.6 |
| Seating | 24,300 | 243 seats. Three-class layout configuration |
|  | Takeoff Analysis |  |
| Payload + OEW | 127,447 |  |
| DTW (desired takeoff weight) | 183,000 | From Payload-Range diagram (Fig. 3.2.9) |
| Fuel load | 55,553 | OK. Less than maximum usable fuel |
| Mean Maximum Temp. of Hottest month | $\begin{aligned} & 75 \text { deg. } \mathrm{F} \\ & 24 \mathrm{deg} . \mathrm{C} \end{aligned}$ | Use ISA + 15 deg. C charts |
| Takeoff Runway Length | $\begin{gathered} 8,500 \mathrm{ft} \\ 2,592 \mathrm{~m} . \end{gathered}$ | Use Figure 3.3.28 <br> Boeing 767-400ER <br> Wet pavement <br> ISA + 15 deg. C |
|  | Landing Analysis |  |
| Landing weight for computation | 158,757 | Value of MALW |
| Landing runway length | $\begin{aligned} & \text { 7,100 ft (flaps } 30 \mathrm{deg} .) \\ & 7,300 \mathrm{ft} \text { (flaps } 25 \mathrm{deg} .) \end{aligned}$ | Use the lowest value (higher flap setting) <br> Figures 3.4.10 and 3.4.9 |

Conclusion: The runway 24R can be used for the LAX-LIM operation.

3.2.9 PAYLOAD/RANGE FOR LONG-RANGE CRUISE

MODEL 767-400ER (CF6-80C2B8 ENGINES)
Figure 1a. Payload-Range Analysis. LAX-LIM Route. Boeing 767-400ER.


### 3.3.28 F.A.R. TAKEOFF RUNWAY LENGTH REQUIREMENTS

STANDARD DAY $+27^{\circ} \mathrm{F}$ (STD $+15^{\circ} \mathrm{C}$ ), WET SMOOTH RUNWAY SURFACE MODEL 767-400ER (CF6-80C2B8F ENGINES)
Figure 1b. Takeoff Analysis. LAX-LIM Route. Boeing 767-400ER.

Table 1c. LAX-HKG Flight. Boeing 777-300ER with General Electric GE90/115BL Engines. 6,624 nm Planned Route Distance.

| Parameter | Value (kg) | Remarks |
| :---: | :---: | :---: |
| MTOW | 351,535 | Table 2.1.1 per Boeing Specification (B777 Manual) |
| MALW | 251,290 | Table 2.1.1 |
| OEW | 167,829 | Table 2.1.1 |
| Max. Payload | 69,853 | Table 2.1.1 |
| Usable Fuel | 145,538 | Table 2.1.1 |
| Seating and passenger load | 37,000 | 370 seats. Three-class layout configuration |
|  | Takeoff Analysis |  |
| Payload + OEW | 204,829 |  |
| DTW (desired takeoff weight) | 324,000 | From Payload-Range diagram (Fig. 3.2.2) |
| Fuel load | 119,171 | OK. Less than maximum usable fuel |
| Mean Maximum Temp. of Hottest month | $\begin{aligned} & 75 \mathrm{deg} . \mathrm{F} \\ & 24 \mathrm{deg} . \mathrm{C} \end{aligned}$ | Use ISA + 15 deg. C charts |
| Takeoff Runway Length | $\begin{gathered} 9,000 \mathrm{ft} \\ 2,744 \mathrm{~m} . \end{gathered}$ | Use Figure 3.3.10 <br> Boeing 777-300ER <br> ISA +15 deg. $C$ |
|  | Landing Analysis |  |
| Landing weight for computation | 251,290 | Value of MALW |
| Landing runway length | $\begin{aligned} & \text { 7,100 ft (flaps } 25 \mathrm{deg} .) \\ & \text { 6,700 ft (flaps } 30 \text { deg.) } \end{aligned}$ | Use the lowest value (higher flap setting) <br> Figures 3.4.5 and 3.4.6 |

Conclusion: The airport needs to lengthen runway 24R to 9,000 feet. However, the longest runway at LAX is 12,091 feet long.


Figure 1c. LAX-HKG Flight. Boeing 777-300ER with General Electric GE90/115BL Engines. 6,624 nm Planned Route Distance.


Figure 1b. Takeoff Analysis. LAX-HKG Flight. Boeing 777-300ER with General Electric GE90/115BL Engines. 6,624 nm Planned Route Distance.

## Problem \# 2 (50 points)

Problem 1
Use the large twin-engine transport aircraft performance file provided in the Matlab files for CEE 5614 (http://128.173.204.63/courses/cee5614/matlab files_cee5614.html to answer the following questions.

The aircraft is cruising at FL 330 and Mach 0.80 over the Atlantic Ocean enroute from Santo Domingo (SDQ), Dominican Republic to Madrid (Spain) as shown in Figure 1. The aircraft has a mass of 290,000 kg at the departure airport (SDQ). The takeoff mass is comprised of the following:

Operating empty mass $=140,000 \mathrm{~kg}$
Fuel weight onboard= $100,000 \mathrm{~kg}$
Payload $=50,000 \mathrm{~kg}$ ( 300 passengers $+20,000 \mathrm{~kg}$ of belly cargo in LD3 containers)
The pilot files a flight plan and requests Flight Level 330 for the cruise portion the flight. The aircraft flies to a waypoint position located $1,700 \mathrm{~nm}$ from SDQ (see Figure 1) when the aircraft requests a new cruise flight level to climb to 36000 feet. Assume ISA conditions in the analysis. Figure 1 shows the diversion points if the aircraft where to experience an engine failure.


Figure 1. Situation of the Flight for Problem 2. Source of Map: Google Earth.
a) Calculate the distance flown from Santo Domingo to the TOC point (assume great circle distance flown).
b) Estimate the fuel consumed in the climb procedure. State the climb distance and the climb time.
c) Find the fuel burn to the point when the aircraft climbs to 36,000 feet.
d) Find the total fuel consumed in the journey from SDQ to MAD.

Table 1d. SDQ-MADFlight. Large Twin-Engine Transport Aircraft. 4,370 nm Planned Route Distance (4,162 nm GCD).

| Parameter | Value (kg) | Remarks |
| :---: | :---: | :---: |
| OEW | 140,000 | Given in statement of the problem |
| Fuel on-board | 100,000 |  |
| Passenger load | 50,000 | 300 passengers $+20,000 \mathrm{~kg}$ of belly cargo |
| Takeoff weight | 290,000 |  |
|  | Initial Climb Analysis |  |
| Takeoff weight | 290,000 |  |
| Cruise Altitude | 33,000 | Given in problem statement |
| Time to TOC | 10.9 | minutes |
| Distance to TOC | 61.5 | nm |
| Fuel to TOC | $\begin{aligned} & 24,789 \mathrm{~N} \\ & 2,527 \mathrm{~kg} \end{aligned}$ | Using the unrestricted climb Matlab code provided |
|  | Initial Cruise Analysis |  |
| weight at TOC | 287,473 | kilograms |
| Cruise distance | 1638.5 | In Nautical Miles 3,035 km |
| Cruise speed | $\begin{gathered} \text { Mach } 0.80 @ 33,000 \mathrm{ft} \\ 239.4 \mathrm{~m} / \mathrm{s} \end{gathered}$ | 320 knots IAS |
| Cruise time | 211.3 | minutes |
| Drag in cruise | 155,630 | Newtons @ 33,000 feet and Mach 0.80 |
| Fuel flow | 24.9 | Newtons/second |
| Fuel (initial cruise) | 32,178.4 | kilograms |
| Weight at 1700 nm point | 255,294.6 | kilograms |

Table 1d. SDQ-MADFlight. Large Twin-Engine Transport Aircraft. 4,370 nm Planned Route Distance (4,162 nm GCD).

| Parameter | Value (kg) | Remarks |
| :---: | :---: | :---: |
|  | Step Climb Analysis |  |
| Weight at 1700 nm point | 255,294.6 | Previous calculation |
| Time to Step TOC | 2.83 | minutes <br> from 33,000 to 36,000 feet |
| Distance to TOC | 22 | nm |
| Fuel to TOC | 508.4 | kilograms. Using the unrestricted climb Matlab code provided |
|  | Second Cruise Analysis |  |
| Weight at Step TOC | 254,786.2 | kilograms |
| Cruise distance | 2405 | In Nautical Miles Calculated as: 4370-1715-250 |
| Cruise speed | $\begin{gathered} \text { Mach } 0.80 @ 36,000 \mathrm{ft} \\ 236 \mathrm{~m} / \mathrm{s} \end{gathered}$ | 305 knots IAS |
| Cruise time | 315.0 | minutes |
| Drag in cruise | 138,790 | Newtons @ 36,000 feet and Mach 0.80 |
| Fuel flow | 22.2 | Newtons/second |
| Fuel (second cruise segment) | 42,770.6 | kilograms |
| Weight at TOD | 212,015.6 | kilograms |
|  | Descent Analysis |  |
| Descent Distance | 250.0 | nm |
| Descent fuel | 3,747.0 | kg |
| Final weight | 208,268.6 | kg |
| Total fuel used | 81,731.4 | kilograms |



Figure 2a. Climb Profile for Large Twin Engine Aircraft. Initial Airport Elevation is at Sea Level Conditions. Time to Climb to 33,000 feet is 652 seconds (10.9 minutes).


Figure 2b. Climb Profile for Large Twin Engine Aircraft. Initial Flight Level is 33,000 feet. Time to Climb to 36,000 feet is 120 seconds (2 minutes). Mach 0.80 Climb Speed.


Figure 2c. Climb Profile for Large Twin Engine Aircraft. Initial Flight Level is 33,000 feet. Distance to Climb to 36,000 feet is 15 nm . Mach 0.80 Climb Speed.


Figure 2d. Descent Profile. Large Twin Transport Aircraft.

