

Assignment 2: Basic Performance Calculations

Date Due: January 30, 2018

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Problem 1

Use the Matlab computer program ISAM.m (available in the Matlab files section of our web site - http://128.173.204.63/courses/cee5614/matlab_files_cee5614.html) to answer the following questions:

- a) An Airbus A380 of Singapore Airlines (Flight SIA 25) flew on January 22, 2018 from JFK to Frankfurt at Mach 0.845 and at 39,000 feet over the North Atlantic. Assuming ISA conditions, find the true airspeed (in knots) of the aircraft and the typical outside temperature at the cruise altitude (Flight Level 390).

Sol: 485 knots

- b) An Air Canada Express Bombardier CRJ-200 pilot reads 245 knots indicated airspeed while descending through 12,000 feet near Montreal Airport. Estimate the value of true airspeed under ISA conditions.

Sol: 280 knots

- c) If the the Flight Management Computer (FMS) for SIA flight 25 reports a 65 knot tailwind when the aircraft in part (b) cruises at FL390. Find the ground speed of the aircraft.

Sol: 550 knots

Problem 2

A United Express Embraer 175 departs Raleigh-Durham airport. The pilot in command follows the following indicated speed profile.

- a) Estimate the true airspeeds (TAS) for each one of the points in the climb profile. Assume ISA atmospheric conditions and zero wind in your calculations. Plot the values of TAS vs altitude.

Table 1. Indicated Speed Profile for Embraer 175 departing RDU Airport.

Altitude (meters)	Indicated Airspeed (knots)	True Air Speed (knots) Rounded to Nearest Knot
133	160	161
1,500	185	195
2,200	195	211
3,100	240	269
5,200	260	315
6,800	265	341
7,400	270	356
8,600	280	386
9,146	280	395

- b) Find the Mach number immediately after departure from RDU runway 23R and at the top of climb point (TOC).

Sol: at 133 meters Mach = 0.25
Sol: at 9,146 meters, Mach = 0.67

c) Estimate the true airspeed of the aircraft at 10,000 feet.

Sol: Interpolate from Table 1 to get 266 knots

Problem 3

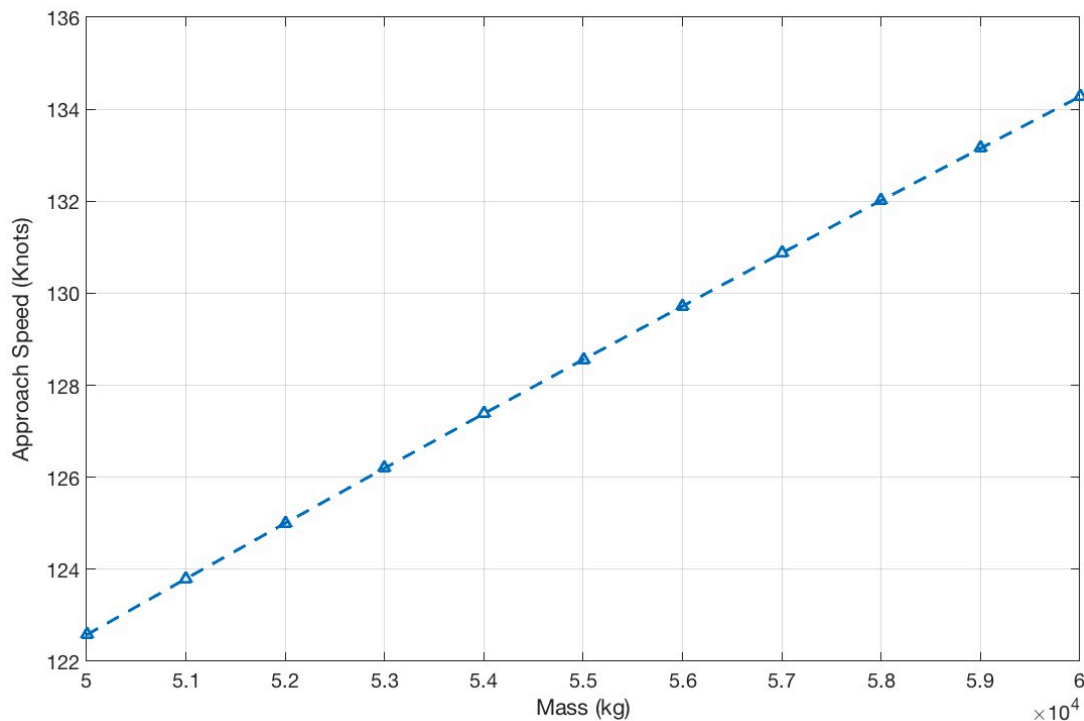
The minimum flight speed achievable in steady-flight (called stalling speed V_{stall}) can be estimated using the fundamental lift equation:

$$V_{stall} = \sqrt{\frac{2mg}{\rho S C_{l_{max}}}}$$

where: m is the aircraft mass (in kilograms), g is the gravity constant (9.81 m/s-s), S is the aircraft wing area (square meters), ρ is the air density (kg/cubic meter) and $C_{l_{max}}$ (dimensionless) is the maximum lift coefficient (a parameter determined by the aerodynamic capability of the aircraft). According to Federal Aviation Regulations (FAR Part 121), the approach speed of an aircraft should be 1.3 times the stalling speed. According to the same regulations, the initial safe climb speed is 1.2 times the stalling speed after takeoff.

Estimate the stalling and approach speeds for a commonly used twin-engine, jet aircraft with the following parameters: $S = 127$ square meters, $C_{l_{max}} = 2.68$ (with flaps down 30 degrees in the landing configuration), landing mass of 66,800 kg (the maximum allowable landing mass) and landing at sea level ISA atmospheric conditions. Note that all speeds calculated using this method are true airspeeds.

a) Repeat the analysis of part (a) for landing mass of 50,000, 55,000 and 60,000 kilograms. Plot the trend of landing speeds.



b) Repeat the analysis for altitudes ranging from sea level to 3,000 meters (every 500 meters). Comment of the observed trends and also comment on how landing distance is affected by airport elevation.

Sol: Approach speeds increase. For example, at 3,000 meters and 50,000 kilograms, the approach speed is now 142.3 knots (instead of 122.6 knots). Almost a 20 knot increase. Runway length increases non-linearly.

c) If the same aircraft has a $C_{l_{max}} = 1.75$ (with flaps down 10 degrees in the takeoff configuration), find the initial safe climb speed at the maximum takeoff mass of 78,000 kilograms. Repeat for values of takeoff mass ranging from 65000 to 78,000 kilograms.

