# **CEE 3804 Assignment 7 Solution**

### Problem 1

a) and b)

```
%% Problem 1 a)
t=0:0.02:20;
y=1.5+t.^(1.2).*exp(-t);
ha=plot(t,y);
grid on
xlabel('Time (s)')
ylabel('Horizontal Building Displacement (cm)')
%% Problem 1 b)
ha.LineWidth=1.5;
ha.Marker='o';|
ha.Color=[0 0.4470 0.7410];
```







```
%% Problem 1 c)
z=gradient(y,0.02);
subplot(2,1,1)
hc1=plot(t,y);
hc1.Color='b';
xlabel('Time (s)')
ylabel('Horizontal Building Displacement (cm)')
grid on
subplot(2,1,2)
hc2=plot(t,z);
hc1.Color='r';
grid on
xlabel('Time (s)')
ylabel('Gradient')
```

d) and e)

Peak: y= 1.8749 z= 3.4709e-05 (very close to zero)

The time when it happens t=1.20 seconds

```
%% Problem 1 d) and e)
[max_disp,index]=max(y);
z_at_peak=z(index);
time_max_disp=t(index);
```

Problem 2

a) and b)

```
%% Problem 2 a) and b)
warning('off')
USdam=readtable('C:\CEE 3804\HW7\US_dams_2023.xlsx','Sheet','damData');
```

c) and d)

```
Regression y= 29.796*x+2432.4 R<sup>2</sup>=0.362
```



```
%% Problem 2 c) and d)
h1=scatter(USdam.SurfaceArea,USdam.NormalStorage);
grid on
hold on
xlabel('SurfaceArea')
ylabel('NormalStorage')
mdl=fitlm(USdam.SurfaceArea,USdam.NormalStorage);
NormalStorage_prediction=predict(mdl,USdam.SurfaceArea);
h2=plot(USdam.SurfaceArea,NormalStorage_prediction);
legend([h1 h2],'Original','Regression')
```

e) The most frequent height of US dams is in the range between 50  $\sim$  60 feet.



g) The number of dams in the state of Virginia: 130

```
%% Problem 2 e)
histogram(USdam.Height)
xlabel('Height (feet)')
%% Problem 2 f)
Dam_CA=USdam.Name(strcmp(USdam.State,'CA'));
%% Problem 2 g)
Num_Dam_VA=sum(strcmp(USdam.State,'VA'));
```

#### Problem 3

a) and b)

There are 8 stops.

```
%% Problem 3 a) and b)
warning('off')
GPSData=readtable('C:\CEE 3804\HW7\GPSData_a7_blank.xls','Sheet','GPS Car Data');
plot(GPSData.Time_s_,GPSData.Speed_km_h_)
xlabel('Time (seconds)')
ylabel('Speed (km/h)')
```



c) and d)

```
%% Problem 3 c) and d)
```

GPSData.Speed\_meter\_sec\_=GPSData.Speed\_km\_h\_\*1000/3600; GPSData.Speed\_miles\_h\_=km2sm(GPSData.Speed\_km\_h\_);

```
e)
```

```
%% Problem 3 e)
GPSData.Acceleration = gradient(GPSData.Speed_km_h_,2);
plot(GPSData.Time_s_,GPSData.Acceleration)
xlabel('Time')|
ylabel('Acceleration')
```



f), g), and h)

The largest speed during the journey: 70.7 km/hr.

The time when the maximum speed is recorded are: 692 and 1332 seconds.

The average speed in miles per hour: 28.58 mph

The number of seconds the car is traveling below 15 mph: 284 seconds or 142 intervals, the vehicle is below 15 mph.

```
%% Problem 3 f), g), and h)
[max_speed,~]=max(GPSData.Speed_km_h_);
idx=find(GPSData.Speed_km_h_==max_speed);
time_max_speed=GPSData.Time_s_(idx);
disp(max_speed)
disp(time_max_speed)
average_speed_miles_hour=mean(GPSData.Speed_miles_h_);
num seconds less 15mph=length(find(GPSData.Speed_miles h <=15));</pre>
```

The num\_seconds\_less\_15mph is really the number of instances that Matlab finds the speed below 15. However, the quantity needs to be multiplied by 2 because very time interval is 2 seconds.

Number of seconds below 15 mph = 284 seconds

```
Number of instances below 15 mph = 142
```

#### **Problem 4**

Task 1

 $3x_1 + 4x_2 + x_3 + 6x_4 = 25$   $2x_1 + 9x_2 + 7x_3 + 13x_4 = 36$   $6x_1 + 5x_2 + 3x_3 + x_4 = 21$  $3x_1 + 8x_2 + 9x_3 + 3x_4 = 13$ 

Define the system of equations as:

A=[3 4 1 6; 2 9 7 13; 6 5 3 1; 3 8 9 3];

b=[25 36 21 13]'

The solution of the system of equations is:

X=A\b

x =

2.8446

1.0473

-1.1824

2.2432

The same result is obtained if we use the inverse function in Matlab.

x= inv(A)\*b

Task 2

```
%% Problem 4 Task 2
C=[5 2 1 6;2 9 7 13;6 5 3 1;7 8 9 3];
D=[1 5 2 6]';
E=C*D;
det(C);
inv(C);
F = (C+25)/3;
G = diag(C);
S = inv(C)*D;
T = ones(4,4) + C;
first_row_C=C(1,:);
last_column_C=C(:,end);
```

a) E = 53 139 43

83

## b) 1.4840e+03

c)

0.1509	-0.0802	0.0236	0.0377
-0.2372	0.1260	0.3915	-0.2022
0.0566	-0.0613	-0.3349	0.2642
0.1105	0.0350	-0.0943	-0.0081

## d) and e)

F =

10.0000	9.0000	8.6667	10.3333
9.0000	11.3333	10.6667	12.6667
10.3333	10.0000	9.3333	8.6667
10.6667	11.0000	11.3333	9.3333

### G =

# f) and g)

S =

0.0236 -0.0371 0.6651 0.0485

### Т =

6	3	2	7
3	10	8	14
7	6	4	2
8	9	10	4

# h) and i)

first\_row\_C = 5 2 1 6

last\_column\_C =