## Assignment 5: Basic Matlab Operations Solution

Date Due: October 11, 2013
Instructor: Trani

## Problem 1

Use Matlab to solve this problem. Use the Command Window and define two matrices, A and B, in Matlab. Use (;) to separate the rows in the matrix and use square parenthesis to define the numerical values inside the matrix.
$A=\left[\begin{array}{lll}7 & 8 & 1 \\ 4 & 6 & 1 \\ 9 & 8 & 6\end{array}\right]$
and $B=\left[\begin{array}{lll}13 & 12 & 5\end{array}\right]$
Perform the following matrix operations. In one line comment on the results obtained after each operation.
a) $C=B \times A$
b) $D=A(1,:)$
c) $E=2 * B^{\prime}$
d) $F=A \times B$
e) $G=A(3,:)+B$
f) $H=A(:, 1)$ compare with part (b). Comment.
g) $I=\operatorname{diag}(A)+B^{\prime}$
h) $J=\operatorname{ones}(3,3)+A$
i) $x=\operatorname{inv}(A) * B^{\prime}$

Answer:
a) $\mathrm{C}=\left[\begin{array}{lll}184 & 216 & 55\end{array}\right]$;

If use cross() function, it will be an error.
b) $D=\left[\begin{array}{lll}7 & 8 & 1\end{array}\right]$;
c) $E=[26 ; 24 ; 10]$;
d) $\mathrm{F}=$ error, Inner matrix dimensions must agree.
e) $G=\left[\begin{array}{lll}22 & 20 & 11\end{array}\right]$;
f) $H=[7 ; 4 ; 9]$; Comment: part (b) got the first row of Matrix A, while part (f) got the first column of Matrix A.
g) $\mathrm{I}=[20 ; 18 ; 11]$;
h) $J=\left[\begin{array}{lllllll}8 & 9 & 2 ; 5 & 7 & 2 ; 10 & 9 & 7\end{array}\right]$;
i) $x=[-1.9630 ; 3.4444 ;-0.8148]$.

Comment:
The Matlab can easily do matrix calculation. But the calculation should obey the matrix calculation rules, such as when doing matrix multiply matrix, the inner matrix dimensions must agree.

## Problem 2

Use Matlab to solve this problem.
a) Create a new Matlab script and define two vectors as follows:
$x=0: 0.1: 20$
$y=x . \wedge 1.85 . * \exp (-x)$
In your script make a simple plot using the "plot" function in Matlab. Label the $x$-axis as 'Time (seconds)' and the $y$ axis as 'Amplitude (dim)'. Add a grid to the plot using the 'grid' attribute of the plot.
Answer:

b) Modify the script created in part (a) and using the interactive 'Tools-Edit Plot' adjust the color of the line to be red and the line width to be 4.0.

Answer:


c) Modify the script created in part (a) creating another variable $z$.
$z=\operatorname{gradient}(y) \quad \%$ the Matlab function gradient takes the first derivative of the values in $(y)$
Using the "subplot" command create a new figure with two plots. Plot the values of $x$ vs. $y$ in the upper part of the window and $x$ vs. $z$ in the lower part of the same window. Change the line colors to distinguish the two views.

d) Verify that the "gradient" function is working. Verify a few numbers by hand if necessary.

Answer:
The gradient near $x=1.8$ is close to 0 . And obviously, the gradient at $x=1.8$ is close to 0 .

## Problem 3

Use Matlab to solve this problem. A companion file provided in the assignment contains the population of the top 25 cities in the US.

| Rank | City | State | Population in 2012 | Population in 2010 |
| ---: | :--- | :--- | ---: | ---: |
| 1 | New York | New York | 8336697 | 8175133 |
| 2 | Los Angeles | California | 3857799 | 3792621 |
| 3 Chicago | Illinois | 2714856 | 2695598 |  |
| 4 | Houston | Texas | 2160821 | 2100263 |
| 5 | Philadelphia | Pennsylvania | 1547607 | 1526006 |
| 6 | Phoenix | Arizona | 1488750 | 1445632 |
| 7 San Antonio | Texas | 1382951 | 1327407 |  |
| 8 San Diego | California | 1338348 | 1307402 |  |
| 9 | Dallas | Texas | 1241162 | 1197816 |
| 10 | San Jose | California |  | 982765 |
| 11 | Austin | Texas |  | 842592 |

a) Crete a Matlab script and read the data using the Import Wizard in Matlab.

b) Create variables for each column of data provided. For example, Column 1 is the "Rank" variables, and so on.
c) Create a new variable in the scrip to estimate the change in population between the years 2012 and 2010.

| $\square$ diff_Pop < $25 \times 1$ double> |  |  |
| :---: | :---: | :---: |
|  | 1 | 2 |
| 1 | 161564 |  |
| 2 | 65178 |  |
| 3 | 19258 |  |
| 4 | 60558 |  |
| 5 | 21601 |  |
| 6 | 43118 |  |
| 7 | 55544 |  |
| 8 | 30946 |  |
| 9 | 43346 |  |
| 10 | 36823 |  |
| 11 | 52202 |  |
| 12 | 14723 |  |
| 13 | 14407 |  |
| 14 | 20628 |  |
| 15 | 22765 |  |
| 16 | 36786 |  |
| 17 | 43778 |  |
| 18 | -12302 |  |
| 19 | 23417 |  |
| 20 | 8266 |  |
| 21 | 18885 |  |
| 22 | 25875 |  |
| 23 | 34107 |  |
| 24 | 30600 |  |
| 25 | 23274 |  |

d) Find the percent change (\%) of the population between the two years.

| $\square$ Per_Pop < $25 \times 1$ double> |  |  |
| :---: | :---: | :---: |
|  | 1 | 2 |
| 1 | 1.0198 |  |
| 2 | 1.0172 |  |
| 3 | 1.0071 |  |
| 4 | 1.0288 |  |
| 5 | 1.0142 |  |
| 6 | 1.0298 |  |
| 7 | 1.0418 |  |
| 8 | 1.0237 |  |
| 9 | 1.0362 |  |
| 10 | 1.0389 |  |
| 11 | 1.0660 |  |
| 12 | 1.0179 |  |
| 13 | 1.0176 |  |
| 14 | 1.0256 |  |
| 15 | 1.0289 |  |
| 16 | 1.0496 |  |
| 17 | 1.0599 |  |
| 18 | 0.9828 |  |
| 19 | 1.0361 |  |
| 20 | 1.0128 |  |
| 21 | 1.0306 |  |
| 22 | 1.0425 |  |
| 23 | 1.0568 |  |
| 24 | 1.0509 |  |
| 25 | 1.0387 |  |

e) Find the name of the city with the highest population change using the Matlab "max" function (e.g.,, max(x) finds the highest value of vector x )

Answer:

Austin, (change $=106.6 \%$ ) had the highest percent change; while New York had the highest change in absolute value of population (change $=161564$ ).
f) Find the names of the top 25 cities located in the state of California. Show the code to do this search. I suggest you use the "find" function in Matlab as demonstrated in class.

| 6 | CityCA $<4 \times 1$ | cell> |
| :--- | :--- | :--- |
|  | 1 | 2 |
| 1 | Los Angeles |  |
| 2 | San Diego |  |
| 3 | San Jose |  |
| 4 | San Franci... |  |

## Problem 4

Data collected by a Global Positioning System (GPS) recording unit inside a car is presented in the accompanying file (GPS Data). Create a Matlab script that performs the following steps:
a) Import the data into Matlab using the "load" command.
b) Plot the speed of the car (in $y$-axis) vs. time ( $x$ - axis). Observe the plot and comment on the number of stops the vehicle makes.
c) Estimate the acceleration of the car as a function of time (use the Matlab "gradient" function - see Problem 2). In your script find the largest deceleration the vehicle makes and the time where that acceleration is recorded. Comment on the driving behavior of the person driving the vehicle.
d) Find the average speed of the car for the complete profile. Use the Matlab function $\operatorname{MEAN}(x)$ to get the average speed.
e) Find the number of seconds the car spends at a red traffic light.

Answer:
a)
b)


Comment:
The car makes 4 stops, which are around $\underline{100 \mathrm{~s}, 340 \mathrm{~s}, 490 \text { s and } 750 \mathrm{~s} \text {. }}$
c)

Comment:
The vehicle may travel in an urban area, where it hit the red light for several times. So the vehicle has to accelerate and decelerate frequently.
d)

e)

The car spends $\mathbf{1 1 4 \mathbf { s }}$ at a red traffic light.

