## CEE 3804 Exam2 (Spring 2024)

# Computer Applications in Civil Engineering 

## Open Book and Notes -

Your Name $\qquad$

Your Signature * $\qquad$

* The answers in this exam are the product of my own work. I certify that I have not received nor I have provided help to others while taking this examination.


## Directions:

Solve the problems. Copy and paste the computer code and solutions such as graphs in a Word Document and convert to a single PDF file. Make sure your code is not too small for me to be able to read it. Minimum font size 10.

## Problem 1 (30 points)

Electric and natural gas-powered vehicles require charging stations along highways in the United States. Figure 1 shows sample data for several types of charging stations including electric (ELEC) and natural gas (CNG) stations.

|  | A | B | C | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Fuel Type Code | Station Name | Street Address | ntersection Directions | City | State | Latitude | Longitude |
| 2 | CNG | Arkansas Oklahoma Gas | 2100 S Waldron Rd |  | Fort Smith | AR | 35.36 | -94.38 |
| 3 | CNG | Clean Energy - Logan Inte | 1000 Cottage St Ext | From Route 1, take the | East Boston | MA | 42.37 | -71.03 |
| 4 | CNG | Clean Energy - Everett - N | 16 Rover St | Rt 16, exit to Rt 99, to D | Everett | MA | 42.39 | -71.06 |
| 5 | CNG | Clean Energy - Greenpoin | 287 Maspeth Ave | I-278/Brooklyn Queens | Brooklyn | NY | 40.72 | -73.93 |
| 6 | CNG | Canarsie - National Grid | 8424 Ditmas Ave | From Shore Pkwy, tak | Brooklyn | NY | 40.65 | -73.92 |
| 7 | CNG | Con Edison - Van Nest Seı | 1615 Bronxdale Ave | Hutchinson River Park | Bronx | NY | 40.84 | -73.86 |
| 8 | CNG | Con Edison - Rye Service 1 | 178 Theodore Fremd Ave | 1-95/New England Thrl |  | NY | 40.98 | -73.69 |
| 9 | CNG | Con Edison-College Poin | 124-1531st Ave | From I-678/Whiteston | Queens | NY | 40.77 | -73.84 |
| 10 | CNG | CNG Source Fueling - Gre | 111 W Raymond St | 1-65, exit onto Raymon | Indianapolis | IN | 39.74 | -86.16 |
| 11 | CNG | Black Hills Energy | 1301 W 24th St | From I-25 take exit 10, | Cheyenne | WY | 41.14 | -104.83 |
| 12 | CNG | Clean Energy - City of San | 2931 Rufina St |  | Santa Fe | NM | 35.66 | -105.99 |
| 13 | CNG | Kansas Gas Service | 11401 W 89th St | Station located in Servi | Overland Park | KS | 38.97 | -94.72 |
| 14 | CNG | Kansas Gas Service | 200 E 1st Ave |  | Topeka | KS | 39.06 | -95.67 |

## Figure 1. Sample Car Power Station Data.

a) Create a Matlab script to read the data. Label the variables appropriately and include their units if applicable as part of the variable name.

| 7 | \% Auto-generated by MATLAB on 12-Apr-2024 17:11:34 |
| ---: | :--- |
| 8 |  |
| 9 | \%\% Set up the Import Options and import the data |
| 10 | opts = spreadsheetImportOptions("NumVariables", 8); |
| 11 |  |
| 12 | \% Specify sheet and range |
| 13 | opts.Sheet = "Data"; |
| 14 | opts.DataRange = "A2:H3803"; |
| 27 | \%\% Convert to output type |
| 28 | FuelTypeCode = tbl.FuelTypeCode; |
| 29 | StationName = tbl.StationName; |
| 30 | StreetAddress = tbl.StreetAddress; |
| 31 | IntersectionDirections = tbl.IntersectionDirections; |
| 32 | City = tbl.City; |
| 33 | State = tbl.State; |
| 34 | Latitude = tbl.Latitude; |
| 35 | Longitude = tbl.Longitude; |

Figure 2. Matlab code to read the data in vector form (independent vectors for each column).
b) Add code the Matlab script created in part (a) to extract all electric charging stations (designated as ELEC in the fuel type code. Provide a list of the first 15 station names so that I can verify that the code works.


Figure 3. Matlab code to extract the electric stations.
The bottom section shows the first 15 electric stations.
c) Use the US map provided in assignment 7 to plot the locations of the electric charging stations. Label them with a red marker.

```
48 % Part (c) get a US map and plot the electric stations
49- % Load the US map provided in class
5 0 ~ l o a d ~ u s a m a p ~
51
5 2 ~ \% ~ M a k e ~ a ~ p l o t ~ a n d ~ h o l d ~ t h e ~ p l o t
5 3
54 plot(uslon,uslat)
55 xlabel("Longitude (deg.)")
56 ylabel("Latitude (deg.)")
57 hold on
58
5 9 ~ \% ~ O b t a i n ~ t h e ~ l a t i t u d e ~ a n d ~ l o n g i t u d e s ~ o f ~ e a c h ~ e l e c t r i c ~ s t a t i o n s
61 longitudeElectricStation = Longitude(indicesElectricStations);
62 latitudeElectricStation = Latitude(indicesElectricStations);
6 3
6 4 ~ p l o t ( l o n g i t u d e E l e c t r i c S t a t i o n , l a t i t u d e E l e c t r i c S t a t i o n , ' + r ' )
```



Figure 4. Matlab code to plot the US map. The data was extracted from an EPA database. It is clear that many stations do not have the correct latitude and longitude coordinates. I used a red + marker instead.
d) Add code to item (b) to calculate the number of CNG stations in the data. The calculation should be done in code. Display the answer in the Command window.

```
67 % Part (d) get CNG stations
68
69 matchCNG = strcmp(FuelTypeCode,'CNG');
70 indicesCNGStations = find(matchCNG); % Indices of the electric stations
71 countCNGStations = length(indicesCNGStations );
72
73 % Display the number of CNG stations
74 clc
75 disp(['Number of CNG Stations = ',num2str(countCNGStations)])
```


## Command Window

## Number of CNG Stations $=65$ <br> $f x \gg$

Figure 5. Matlab code to calculate the number of CNG stations.
e) Add code to item (b) to calculate the number of electric stations in the state of New York. The calculation should be done in code. Display the answer in the Command window.

```
    % Part (e) get the electric stations in the state of New York
    matchElectricNY = strcmp(FuelTypeCode,'ELEC') & strcmp(State,'NY');
    indicesElectricStationsNY = find(matchElectricNY); % Indices of the electric stations in NY
    countElectricNYStations = length(indicesElectricStationsNY);
    % Display the number of CNG stations
    clc
    disp(['Number of Electric Stations in New York = ',num2str(countElectricNYStations)])
```

Number of Electric Stations in New York $=173$ $f_{x} \gg$

Figure 6. Matlab code to calculate the number of stations in New York. Note that I used a combination of the strcmp command and the \& command in Matlab (\& $=$ AND) in line 70 of the code.

## Problem 2 (40 points)

The Manning equation is an empirical relationship used by civil engineers to estimate the flow characteristics inside pipes and channels. Figure 7 shows a simple rectangular channel.


Figure 7. Simple Rectangular Channel.

For a rectangular channel, the following formulas apply.
$A=b y$
\% Area of the flow ( $\mathrm{ft}^{2}$ )
$P=b+2 y$
\% Wetted perimeter (ft)
$R=\frac{b y}{b+2 y}$
\% Hydraulic radius (ft)

The hydraulic radius, $R$ is the quotient of the cross sectional area to the wetted perimeter, $R=A / P$.
The basic Manning Equation is:
$Q=\left[1.486 A * R^{2 / 3} * S^{1 / 2}\right] / n$
Where:
$Q$ is the discharge (cu. feet per second)
$R$ is the hydraulic radius in feet (area of section / wetted perimeter)
$S$ is the slope of the pipe $(\mathrm{ft} / \mathrm{ft})$
$A$ is the cross-sectional area of the flow $\left(\mathrm{ft}^{2}\right)$
$n$ is the pipe roughness coefficient (see table below).

| Type of Pipe | Roughness Coefficient |
| :---: | :---: |
| Concrete and asbestos | 0.012 |
| Corrugated metal | 0.023 |

a) Create a Matlab script to estimate the values of $A, P$, and $R$ given the dimensions of b and y (in Figure 2). Test the code with values of $b=30$ feet and $y=6$ feet.
if strcmp(material,'Concrete')
if strcmp(material,'Concrete')
roughness = 0.012;
roughness = 0.012;
elseif strcmp(material,'Metal')
elseif strcmp(material,'Metal')
roughness = 0.023;
roughness = 0.023;
end
end
\%
\%
$\mathrm{b}=15: 1: 30$; \% base of the open channel (ft)
$\mathrm{b}=15: 1: 30$; \% base of the open channel (ft)
$\mathrm{y}=6$; $\quad$ \% height of channel ( ft )
$\mathrm{y}=6$; $\quad$ \% height of channel ( ft )
\% Calculate the area exposed, wetted perimeter
\% Calculate the area exposed, wetted perimeter
$\%$ and hydraulic radius
$\%$ and hydraulic radius
Area $\quad=\mathrm{b} .{ }^{*} y ; \quad \%$ area in square feet
Area $\quad=\mathrm{b} .{ }^{*} y ; \quad \%$ area in square feet
Perimeter $\quad=b+2^{*} y ; \quad \%$ wetted perimeter (feet)
Perimeter $\quad=b+2^{*} y ; \quad \%$ wetted perimeter (feet)
Radius = Area ./ Perimeter; \% Hydraulic radius (feet)
Radius = Area ./ Perimeter; \% Hydraulic radius (feet)

Figure 8. Code to estimate the area, wetted perimeter and hydraulic radius.
b) Add code to part (a) to estimate Q (discharge) using the Manning equation given all four parameters (A, R, S and n). Test the script for a concrete rectangular channel with the following parameters: $\mathrm{S}=0.002 \mathrm{ft} / \mathrm{ft}$.

```
29 % Formula to calculate the discharge
30
31 Q = ((1.486 * Area .* (Radius .^(2/3) ).* ( slope .^(1/2) ) ) ) ./ (roughness);
32
33 plot(Radius,Q,'o-b')
34 xlabel('Hydraulic Radius (tt^2)')
35 ylabel('Discharge (cu. feet/second)')
36 grid
```

```
Command Window
    Discharge (cu.feet/second) = 2630.1098
fx>> |
```

Figure 9. Code to estimate the discharge (Q).
c)
c) Add code to (a) to estimate the discharge ( Q ) for values of slope ranging from 0.001 to $0.008(\mathrm{ft} / \mathrm{ft})$.

| 6 | \% Define the material of the open channel |
| ---: | :--- |
| 7 | material = 'Concrete'; |
| 8 |  |
| 9 | \% Script to find the Discharge given the hydraulic radius, slope, |
| 10 | \% cross sectional area and roughness. |
| 11 |  |
| 12 | slope = 0.001:0.0005:0.08; |
| 29 | \% Formula to calculate the discharge |
| 30 |  |
| 31 | Q = ( ( 1.486 * Area .* ( Radius .^(2/3) ) .* ( slope .^(1/2) ) ) ) ./ (roughness); |
| 32 |  |
| 33 | plot(slope,Q,'o-b') |
| 34 | title(material) |
| 35 | xlabel('Slope (ft/ft)') |
| 36 | ylabel('Discharge (cu. feet/second)') |
| 37 | grid |




Figure 10. Code to estimate the discharge (Q) for various slopes.
D) In a single graph, plot the values of discharge (Q) for various slopes.

## Problem 3 (30 points)

An engineer formulates a linear programming problem to estimate the number of tons to be produced of two types of concrete mixtures. Figure 11 shows the initial sketch showing a delivery constraint and a production constraint. Both concrete mixes are manufactured with the same equipment. The standard concrete sells for $\$ 1,560$ per ton. The premium concrete sells for $\$ 1,635$ per ton.


Figure 11. Graphical Representation of Concrete Production and Distribution.
a) Write the equations of the linear programming problem. Assume the company wants to maximize the revenue for the company.

Equations:
Maximize $Z=1635 x_{1}+1560 x_{2}$
Subject to:
$1.6 x_{1}+x_{2}<=1700$
$1.15 x_{1}+x_{2}<=1450$
$x_{1}, x_{2}>=0$
b) Solve the problem using Excel Solver. Tell me how many tons of each concrete type should be produced to maximize the profit.

|  | A | B | C | D | E | F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | Decision Variables |  |  |  | - Some |  |
| 4 |  |  |  |  | Srobekere ssor |  |
| 5 | x1 | 0 |  | Number of T | , miover |  |
| 6 | x2 | 1450 |  | Number of T | Smomeratemeosmans |  |
| 7 |  |  |  |  |  |  |
| 8 | Objective Function |  |  |  |  |  |
| 9 |  |  |  |  |  | Reseant |
| 10 | $1635 \times 1+1560 \times 2$ | 2262000 |  |  |  |  |
| 11 |  |  |  |  |  |  |
| 12 | Constraint Equations |  |  |  | Semmeme |  |
| 13 |  | mula |  |  |  |  |
| 14 | $1.6 \times 1+x 2<=1700$ | 1450 |  | 1700 |  |  |
| 15 | $1.15 \mathrm{x} 1+\mathrm{x} 2<=1450$ | 1450 |  | 1450 |  |  |

Figure 12. Excel Solver Solution. The optimal solution is $\mathrm{x} 1=1450$ and $\mathrm{x} 2=0$. The Objective function is $\mathrm{Z}=\$ 2,262,000$.
c) Solve the problem by hand using the Simplex Method. Clearly show your tables and indicate which variables are the basic variables in the current solution.

Adjust the constraint equations by adding one slice variable for each constraint equations.
$\operatorname{Max} Z-1635 x_{1}-1560 x_{2}=0$
$1.6 x_{1}+x_{2}+x_{3}=1700$
$1.15 x_{1}+x_{2}+x_{4}=1450$
$x_{1}, x_{2}, x_{3}, x_{4}>=0$

## Table. Initial Tableau to Solve the Problem.

| BV | Z | X1 | x2 | X3 | X4 | RHS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 1 | -1635 | -1560 | 0 | 0 | 0 |
| X3 | 0 | 1.6 | 1 | 1 | 0 | 1700 |
| X4 | 0 | 1.15 | 1 | 0 | 1 | 1450 |

The basic variables are x 3 , and x 4 . Non-basic variables are X 1 and X 2 . Current solution for $\mathrm{Z}=0$.

| BV | Z | X1 |  | X2 | X3 | X4 | RHS |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Ratio |  |  |  |  |  |  |  |  |
| Z | 1 | -1635 | -1560 | 0 | 0 | 1 |  |  |
| X3 | 0 | 1.6 | 1 | 1 | 0 | 1700 | 1062.5 |  |
| X4 | 0 | 1.15 | 1 | 0 | 1 | 1450 | 1260.9 |  |

Step 2: Select pivot column (column with coefficient for X1 - in yellow).

Step 3: Select the pivot row as the one with the smallest ratio of RHS and picot column coefficients (row in yellow)

Step 4: Perform row operations to zero all elements of pivot column.

| BV | Z | X1 | x2 | X3 | X4 | RHS | Ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 1 | -1635 | -1560 | 0 | 0 | 1 |  |
| X3 | 0 | 1.0 | 0.625 | 0.625 | 0 | 1062.50000 | 1062.5 |
| X4 | 0 | 1.15 | 1 | 0 | 1 | 1450 | 1260.9 |

## Second Tableau.

| BV | Z | X1 | x2 | X3 | X4 | RHS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 1 | 0 | -538.125 | 1021.875 | 0 | 1737188.5 |
| X1 | 0 | 1 | 0.625 | 0.625 | 0 | 1062.5 |
| X4 | 0 | 0 | 0.28125 | -0.71875 | 1 | 228.125 |

$Z=\$ 1737188.5, x 1=1062.5$ and $x 4=228.125, X 3$ and $x 2$ are zero.

Perform the ratio test to determine the pivot row.

| BV | Z | X1 |  | X2 |  | X3 | X4 | RHS |  | Ratio |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: |
| Z | 1 | 0 | -538.125 | 1021.875 | 0 | 1737188.5 |  |  |  |  |
| X1 | 0 | 1 | 0.625 | 0.625 | 0 | 1062.5 | 1700 |  |  |  |
| X4 | 0 | 0 | 0.28125 | -0.71875 | 1 | 228.125 | 811.11 |  |  |  |

Row operations on row 3.

| BV | Z | X1 | x2 | X3 | X4 | RHS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 1 | 0 | -538.13 | 1021.88 | 0.00 | 1737188.50 |
| X1 | 0 | 1 | 0.63 | 0.63 | 0.00 | 1062.50 |
| X4 | 0 | 0 | 1.00 | -2.56 | 3.56 | 811.11 |

## Third Tableau

| BV | Z | X1 |  | X2 |  | X3 |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Z | 1.00 | 0.00 | 0.13 | -353.65 | 1913.78 | 2173769.06 |  |
| X1 | 0.00 | 1.00 | 0.00 | 2.22 | -2.22 | 555.56 |  |
| X2 | 0.00 | 0.00 | 1.00 | -2.56 | 3.56 | 811.11 |  |

## $\mathrm{Z}=\$ 2173769, \mathrm{x} 1=555.6$ and $\mathrm{x} 2=811.1 . \mathrm{X} 3$ and x 4 are zero.

The solution in the third tableau is not optimal. Coefficient of $x 3$ is still negative so the solution can be improved. Introduce variable x3 into the solution and improve $Z$ to reach optimality. The current solution of the third tableau is the intersection of the two constraint equation lines (see Figure 3).

Perform ratio test to determine the pivot row.

| BV | Z | X1 |  | X2 |  | X3 |  | X4 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| RHS | Ratio |  |  |  |  |  |  |  |
| Z | 1.00 | 0.00 | 0.13 | -353.65 | 1913.78 | 2173769.06 |  |  |
| X1 | 0.00 | 1.00 | 0.00 | 2.22 | -2.22 | 555.56 | 250.00 |  |
| X2 | 0.00 | 0.00 | 1.00 | -2.56 | 3.56 | 811.11 | -317.39 |  |

Take the lowest non-negative number of the ratio tests. X3 enters the BV set. X1 leaves the solution.

## Fourth Tableau.

| BV | Z | X1 | x2 | X3 | X4 | RHS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 1.000 | 159.1 | 0.1 | 0.0 | 1,560.2 | 2,262,183.3 |
| X3 | 0.000 | 0.5 | 0.0 | 1.0 | -1.0 | 250.0 |
| X2 | 0.000 | 1.2 | 1.0 | -0.0 | 1.0 | 1,450.1 |

Solution in the fourth tableau is optimal. All Coefficients in the Z-row are positive or zero.
$Z=\$ 2,262,183, x 1=0$ and $x 2=1450 . x 3=250$ and $x 4=0$.
Note: slack variables (x3 or $x 4$ ) can be positive in the optimal solution.
The progression of each solution is shown in Figure 13.


Figure 13. Simplex Method solution. The optimal solution is $x 1=1450$ and $x 2=0$. The Objective function is $Z=\$ 2,262,000$.

